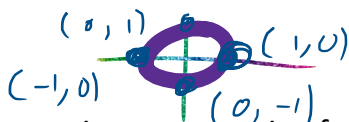


Warm-up!



Solve over $0 \leq \theta < 2\pi$. Then, write an expression for all of the solutions.

Trig Functions, Day 6

- Speed Quiz 3
- More Solving
- (3.12) Pythagorean Identities
- Some notation

Quiz Two Classes From Now

- Solving
- Identities

Homework: Pythagorean Identities

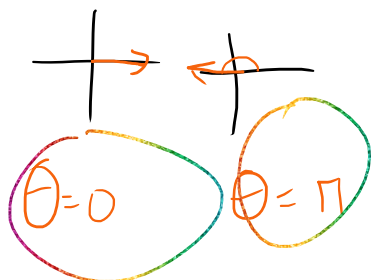
$$(\tan \theta)(\tan \theta + 1) = 0$$

$$\frac{y}{x} = 0$$

$$\tan \theta = 0$$

$$\tan \theta + 1 = 0$$

$$\tan \theta = -1$$



$$\pi - \frac{\pi}{4}$$

$$\theta = \frac{3\pi}{4}$$

$$\theta = \frac{3\pi}{4} + 2\pi k$$

$$\theta = \frac{3\pi}{4} + \pi k$$



$$2\pi - \frac{\pi}{4}$$

$$\theta = \frac{7\pi}{4}$$

$$\theta = \frac{7\pi}{4} + 2\pi k, k \in \mathbb{Z}$$

where k is any integer

$$\theta = 0 + 2\pi k$$

$$\theta = \pi + 2\pi k$$

$$\theta = \pi k$$

Weird thing we sometimes do...

Instead of $(\sin \theta)$, we write...

$$\sin^2 \theta$$

$$\cos^2 \theta = (\cos \theta)^2$$

First, solve over $0 \leq \theta < 2\pi$. Then, write an expression for ALL the solutions.

$$2 \cos^2 \theta + \cos \theta = 0$$

$$2(\cos \theta)^2 + \cos \theta = 0$$

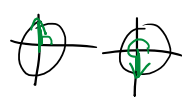
$$(\cos \theta)(2 \cos \theta + 1) = 0$$

$$\cos \theta = 0$$

$$\cos \theta = 0$$

$$2 \cos \theta + 1 = 0$$

$$\cos \theta = -\frac{1}{2}$$



$$\theta = \frac{\pi}{2}$$

$$\theta = \frac{3\pi}{2}$$

$$\theta = \frac{2\pi}{3}$$



$$\theta = \frac{4\pi}{3}$$

$$2K^2 + K = 0$$

$$K(2K + 1) = 0$$

$$K = 0$$

$$\cos \theta = 0$$

$$K = -\frac{1}{2}$$

$$\cos \theta = -\frac{1}{2}$$

$$\theta = \frac{\pi}{2} + 2\pi k \quad \theta = \frac{3\pi}{2} + 2\pi k \quad \theta = \frac{2\pi}{3} + 2\pi k \quad \theta = \frac{4\pi}{3} + 2\pi k, \quad k \in \mathbb{Z}$$



$$\theta = \frac{\pi}{2} + \pi k$$

Solve over $0 \leq \theta < 2\pi$

$$2A^2 - A - 1 = 0$$

$$(2A + 1)(A - 1) = 0$$

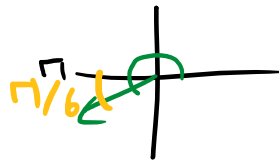
$$A = -\frac{1}{2}$$

$$A = 1$$

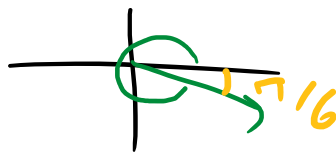
$$2 \sin^2 \theta - \sin \theta - 1 = 0$$

$$\sin \theta = -\frac{1}{2}$$

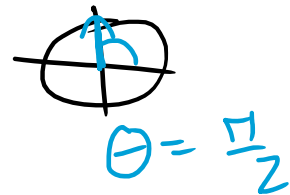
$$\sin \theta = 1$$



$$\theta = \frac{7\pi}{6}$$



$$\theta = \frac{11\pi}{6}$$



First, solve over $0 \leq \theta < 2\pi$. Then, write an expression for ALL the solutions.

$$2 \sin^2 \theta + 3 = 7 \sin \theta$$

The Pythagorean Identities

$$x^2 + y^2 = 1$$

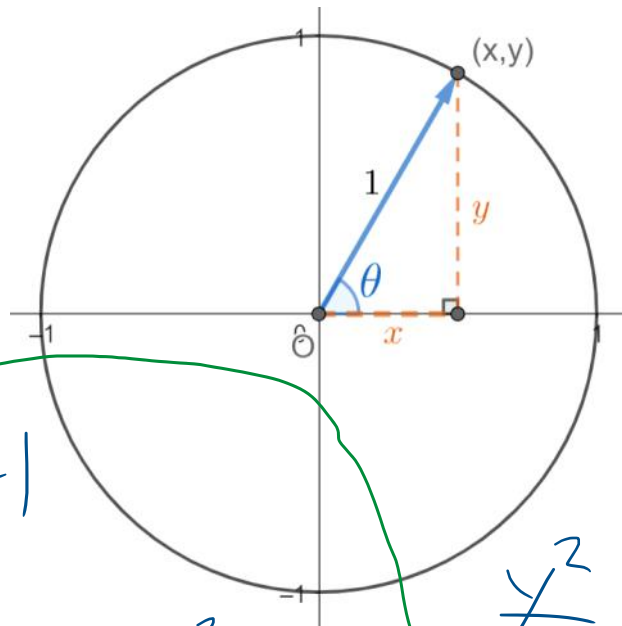
$$(\cos \theta)^2 + (\sin \theta)^2 = 1$$

$$\cos^2 \theta + \sin^2 \theta = 1$$

$$1 + \tan^2 \theta = \sec^2 \theta$$

$$\cot^2 \theta + 1 = \csc^2 \theta$$

$$\cos^2 \theta = 1 - \sin^2 \theta$$



$$\cos \theta = x$$

$$\sin \theta = y$$

$$\tan \theta = \frac{y}{x}$$

$$\sec \theta = \frac{1}{x}$$

$$\csc \theta = \frac{1}{y}$$

$$\cot \theta = \frac{x}{y}$$

$$\frac{y^2}{x^2} = \left(\frac{y}{x}\right)^2$$

Solve over $0 \leq \theta < 2\pi$

$$\boxed{\sin^2 \theta} - \cos \theta - 1 = 0$$
$$1 - \cos^2 \theta - \cos \theta - 1 = 0$$

$$\cos^2 \theta + \sin^2 \theta = 1$$
$$\sin^2 \theta = 1 - \cos^2 \theta$$

$$1 - x^2 - x - 1 = 0$$

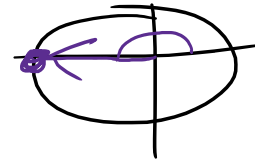
$$-x^2 - x = 0$$

$$x^2 + x = 0$$

$$(x)(x+1) = 0$$

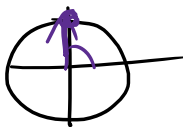
$$x=0 \quad x=-1$$

$$\cos \theta = -1$$

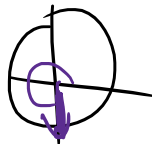


$$\theta = \pi$$

$$\cos \theta = 0$$



$$\theta = \frac{\pi}{2}$$



$$\theta = \frac{3\pi}{2}$$

Solve over $0 \leq \theta < 2\pi$

$$1 + \tan^2 \theta = \sec^2 \theta$$

$$\tan^2 \theta = \sec^2 \theta - 1$$

$$\boxed{\tan^2 \theta} = \sec \theta - 1$$

$$x^2 - 1 = x - 1$$

$$x^2 = x$$

$$x^2 - x = 0$$

$$(x)(x-1) = 0$$

$$x=0 \quad x=1$$

$$\sec^2 \theta - 1 = \sec \theta - 1$$

$$\frac{1}{x}$$

$$\sec \theta = 0$$

impossible

$$\sec \theta = 1$$

$$\cos \theta = 1$$



$$\theta = 0$$

First, solve over $0 \leq \theta < 2\pi$. Then, write an expression for ALL the solutions.

$$\csc \theta \sec \theta - \csc \theta + 2 \sec \theta = 2$$

First, solve over $0 \leq \theta < 2\pi$. Then, write an expression for ALL the solutions.

$$\tan^3 \theta = 3 \tan \theta$$

$$\tan^3 \theta - 3 \tan \theta = 0$$

$$(\tan \theta)(\tan^2 \theta - 3) = 0$$

$$\tan \theta = 0$$



$$\theta = 0 + 2\pi k$$

$$\theta = \pi + 2\pi k$$

$$\theta = \pi k$$

$$\tan^2 \theta - 3 = 0$$

$$\tan \theta = \sqrt{3}$$



$$\theta = \frac{\pi}{3} + 2\pi k$$

$$\theta = \frac{4\pi}{3} + 2\pi k$$

$$\theta = \frac{\pi}{3} + \pi k$$

$$\tan \theta = -\sqrt{3}$$



$$\theta = \frac{2\pi}{3} + 2\pi k$$

$$\theta = \frac{5\pi}{3} + 2\pi k$$

$$\theta = \frac{\pi}{3} k, \quad k \in \mathbb{Z}$$

$$\sin \alpha \cos \alpha = \sin \alpha$$

$$\sin \alpha \cos \alpha - \sin \alpha = 0$$

$$(\sin \alpha)(\cos \alpha - 1) = 0$$

$$\sin \alpha = 0$$

$$\alpha = 0$$

$$\alpha = \pi$$

$$\cos \alpha - 1 = 0$$

$$\cos \alpha = 1$$

$$\alpha = 0$$

